**Harold’s Trig Proofs**

**Cheat Sheet**

15 March 2023

After proving only three (3) trig formulas, we can easily derive **ALL** the trig formulas!

1. Pythagorean Identity
2. Sum and difference formula for sine
3. Sum and difference formula for cosine

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| **Proof of Pythagorean Identities** |
| **Proof** |  |
|  Given | Pythagorean Theorem |
|  Substitute and Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Divide by , then Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Divide by then Simplify |  |
|  Formula |  |

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| **Proof of Sum and Difference Formulas** |
| Trig Sum and Difference Formulas |  |
| Proof Diagram | http://www.themathpage.com/atrig/trig_IMG/128.gif | In VERY simple terms how can I prove the trigonometric identity: Sin (A +  B) = sin A cos B + cos A sin B? - Quora |

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| **Proof of *sin*** |  |
| **Prove Sum** |  |
|  Given |  |
|  Alternate interior angles are congruent |  |
|  Tallest vertical line |  |
|  Substitute, then divide and multiply by AF & FD |  |
|  Convert back to trig formulas |  |
| **Prove Difference** |  |
|  Replace with  |  |
|  Simplify |  |
|  General Formula [4+5] |  |

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| **Proof of**  |  |
| **Prove Sum** |  |
|  Given |  |
|  Longest horizontal line |  |
|  Substitute, then divide and multiply by AF & DF |  |
|  Convert back to trig formulas |  |
| **Prove Difference** |  |
|  Replace with  |  |
|  Simplify |  |
|  General Formula [7+8] |  |

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| **Proof of**  |  |
| **Prove Sum and Difference** |
|  Given |  |
|  Substitute |  |
|  Divide by , then Simplify |  |
|  General Formula |  |

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| **Proof of Double Angle Formulas (2θ)** |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Divide by  |  |
|  Simplify |  |
|  Formula |  |

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| **Proof of Half Angle Formulas (θ/2)** |
| **Proof** |  |
|  Given |  |
|  Solve for  |  |
|  Substitute |  |
|  Solve |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Solve for  |  |
|  Substitute |  |
|  Solve |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Substitute |  |
|  Solve |  |
|  Formula |  |

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| **Proof of Cofunction Formulas** |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |
| **Proof** |  |
|  Given |  |
|  Substitute |  |
|  Simplify |  |
|  Formula |  |